

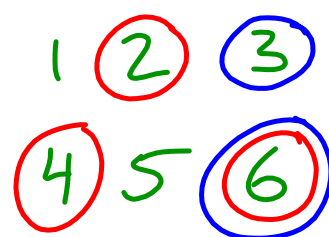
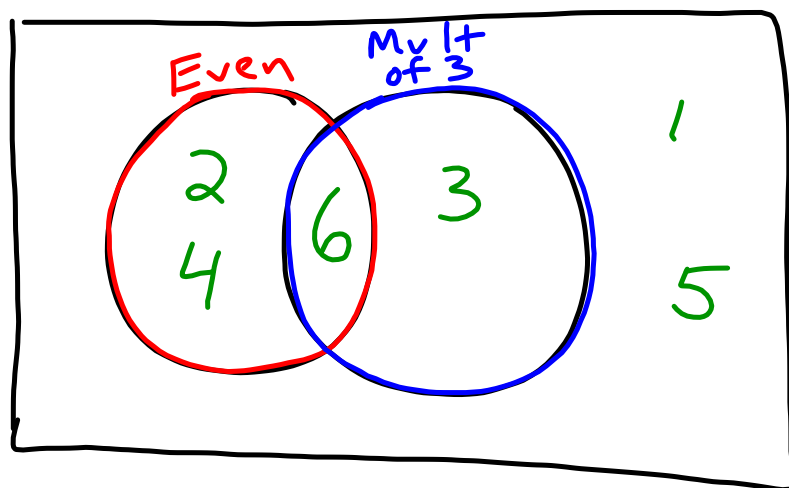
9/11/17 "Success is a journey, not a destination." - Ben Sweetland

HW: "Conditional Probability" homework section #1-4
Test 1 on Tuesday 9/19

AIM: What is Conditional Probability?

Warm Up:
1) On Handout

Either = OR



$$\begin{aligned}
 P(\underset{A}{\text{Even or}} \underset{B}{\text{Mult of 3}}) &= P(\text{Even}) + P(\text{Mult of 3}) - P(\text{Even and Mult of 3}) \\
 &= \frac{3}{6} + \frac{2}{6} - \frac{1}{6} \\
 &= \frac{4}{6} \text{ OR } \frac{2}{3}
 \end{aligned}$$

When the probability of one event occurring changes depending on other events occurring then we say that there is a **conditional probability**. The language and symbolism of conditional probability can be a bit confusing, but the idea is fairly straightforward and can be developed with two-way frequency charts.

Exercise #1: Let's revisit a two-way frequency chart we saw in the last lesson. In this study, 52 graduating seniors were surveyed as to their post-graduation plans and then the results were sorted by gender.

Let the following letters stand for the following events.

M = Male

F = Female

C = Going to College

N = Not going to college

	Gender		Total
	Male	Female	
Going to College	16	13	29
Not Going to College	14	9	23
Total	30	22	52

If a person was picked at random, find the probability that the person was

(a) a female, i.e. $P(F)$

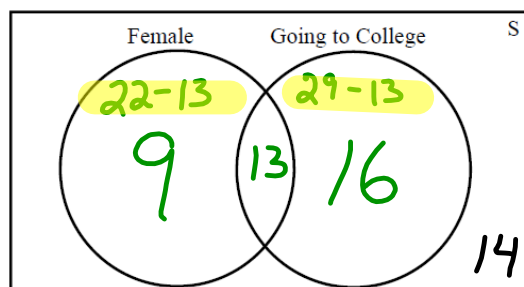
(b) going to college $P(C)$

$$P(F) = \frac{22}{52} \text{ or } 42\%$$

$$P(C) = \frac{29}{52}$$

(c) going to college given they are female, i.e. $P(C|F)$. Draw a Venn diagram below to help justify the ratio that you give as the probability.

$$P(C|F) = \frac{13}{22} \text{ or } 59\%$$



Start with intersection

(d) Which is more likely, that a person picked at random will be going to college, given they are a male, i.e. $P(C|M)$, or that a person will be male, given they are going to college, i.e. $P(M|C)$. Show that calculations for both.

$P(C|M)$

$P(M|C)$

$$P(C|M) = \frac{16}{30} \text{ or } 53\%$$

$$P(M|C) = \frac{16}{29} \text{ or } 55\%$$

30 males
16 of them
going college.

29 people in college
of which 16 are male.

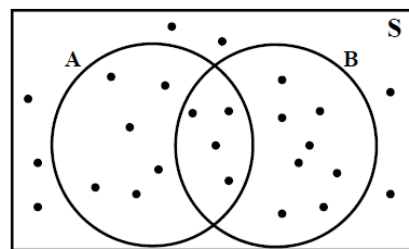
⊗ Formula for Conditional Probability:

$$P(A|B) = \frac{n(A \text{ and } B)}{n(B)} = \frac{n(A \cap B)}{n(B)}$$

$$P(B|A) = \frac{n(A \text{ and } B)}{n(A)} = \frac{n(A \cap B)}{n(A)}$$

We can generalize this process to calculate these conditional probabilities based on counts and a way to calculate these probabilities based on other probabilities.

Exercise #2: In the generic Venn diagram shown to the right. Each dot represents an equally likely outcome of the sample space. Some of these fall only into event A, some only into event B, some in both events and some in neither.



- (a) Consider the probability of A occurring given that B has occurred. Give a formula for this probability based on counting the number of elements in each set and their intersection.

$$P(A | B) =$$

Exercise #3: A survey was taken to examine the relationship between hair color and eye color. The chart below shows the proportion of the people surveyed who fell into each category. If a person was picked at random, find each of the following conditional probabilities. Show the calculation you used.

- (a) Find the probability the person picked had brown eyes given they had blond hair.

$$P(\text{brown eyes} | \text{blond hair})$$

		Hair Color			Total
		Black	Blond	Red	
Eye Color	Blue	0.15	0.20	0.05	0.40
	Brown	0.25	0.10	0.00	0.35
	Green	0.05	0.05	0.15	0.25
	Total	0.45	0.35	0.20	1.00

- (b) Find the probability the person had red hair given they had green eyes.

$$P(\text{red hair} | \text{green eyes})$$

- (c) Does having red hair seem have some **dependence** on having green eyes? How can you tell or quantify this dependence?